1) A direction field for the differential equation $y^{\prime}=y\left(1-\frac{1}{4} y^{2}\right)$ is shown.

a) Sketch the graphs of the solutions that satisfy the given initial conditions.
i. $\quad y(0)=1$
ii. $\quad y(0)=-1$
iii. $y(0)=-3$
iv. $\quad y(0)=3$
b) Find all the equilibrium solutions. $y=0, y=-2, y=2$

Match the differential equation with its direction field (labeled I-IV). Give reasons for your answer.
2) $y^{\prime}=y-1$

IV
3) $y^{\prime}=y-x$

II
4) $y^{\prime}=y^{2}-x^{2} \quad$ III
5) $y^{\prime}=y^{3}-x^{3} \quad$ I

6) Sketch a direction field for the differential equation $y^{\prime}=1+y$. Then sketch the solution curves that go through the points $(0,0),(0,-1),(0,-2)$.

7) Sketch the direction field of the differential equation $y^{\prime}=y-2 x$. Then sketch the solution curve that passes through the point $(1,0)$.

| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 1 | 3 | 1 | 1 | - | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 2 | 1 | - | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | -1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| -31 | 1 | -2 | 1 | $-x$ | 1 | 0 | 1 | 11 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | - | -1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | -1 | 1 | 1 | 1 | 1 | 1 | 1 |  |  |
| 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |  |
| 1 | 1 | 1 | 1 | - | 1 | -2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |  |
| 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |  |
| 1 | 1 | 1 | - | 1 | 1 | -3 |  |  |  |  |  |  |  |
| 1 | 1 | 1 | - | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |  |  |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 |  |  |  |  |  |  |  |

